

Inference at \* 1 1 1  
of proof for Lemma inv\_image\_ind\_tp:

1.  $T : \text{Type}$
2.  $r : T \rightarrow T \rightarrow \mathbb{P}$
3.  $S : \text{Type}$
4.  $f : S \rightarrow T$
5.  $\text{WellFnd}\{\text{i}\}(T; x, y. r(x, y))$
6.  $P : S \rightarrow \mathbb{P}$
7.  $\forall j:S. (\forall k:S. r(f(k), f(j)) \Rightarrow P(k)) \Rightarrow P(j)$
8.  $n : S$

$\vdash P(n)$   
by (%S%  
\p.let x = get\_distinct\_var 'x' p  
inlet n = get\_var\_arg 'n' p

in let S = get\_term\_arg 'S' p  
inlet T = get\_term\_arg 'T' p

in let f = get\_term\_arg 'f' p  
in  
Assert  
 $(\text{mk\_all\_term } x \text{ T}$   
 $\quad ($   
 $\text{mk\_all\_term } n \text{ S}$   
 $\quad (\text{mk\_implies\_term}$   
 $\quad (\text{mk\_equal\_term } T \text{ ($   
 $\text{mk\_apply\_term } f \text{ (mvt } n \text{)} \text{ (mvt } x \text{)})$   
 $\quad (\text{concl } p))) \text{ p})$

1: ....assertion..... NILNIL

2:  
 $\vdash \forall x:T, n:S. (f(n) = x) \Rightarrow P(n)$

9.  $\forall x:T, n:S. (f(n) = x) \Rightarrow P(n)$   
 $\vdash P(n)$